

MATH 152  
Mrs. Bonny Tighe

**QUIZ 3**  
7.5-7.7  
25 points

NAME \_\_\_\_\_  
SECTION \_\_\_\_\_ Wed 9/21/05

1. Differentiate the following.

a)  $y = \cosh^{-1}(\cos^{-1}\sqrt{x})$

b)  $f(x) = \arctan(\csc x)$

c)  $f(x) = \sin^{-1}(x^3)$

d)  $f(x) = (\cos^{-1}x)(\tanh^{-1}x)$

2. Find the numerical value of each expression:

a)  $\cos(\sin^{-1}\frac{\sqrt{3}}{2}) = \underline{\hspace{2cm}}$       b)  $\sinh(0) = \underline{\hspace{2cm}}$       c)  $\cos^{-1}(1) = \underline{\hspace{2cm}}$

3. Simplify: a)  $\sin(\tan^{-1}\frac{5}{12}) = \underline{\hspace{2cm}}$       b)  $\sin(\tan^{-1}x) = \underline{\hspace{2cm}}$

4. Evaluate: a)  $\int \frac{\tan^{-1}x}{1+x^2} dx = \underline{\hspace{2cm}}$       b)  $\int \frac{e^{2x}}{\sqrt{1-e^{4x}}} dx$

$$c) \int \frac{1}{x\sqrt{9x^2 - 1}} dx = \underline{\hspace{2cm}}$$

$$d) \int_0^1 \frac{1}{\sqrt{16x^2 + 1}} dx = \underline{\hspace{2cm}}$$

5. Find the limit. Use L'Hospital's Rule where appropriate. If there is a more elementary method, consider using it. If L'Hospital's Rule doesn't apply, explain why.

$$a) \lim_{x \rightarrow 0^+} (\tan 3x)^x = \underline{\hspace{2cm}} \quad b) \lim_{x \rightarrow \infty} \frac{x^3}{e^x} = \underline{\hspace{2cm}} \quad c) \lim_{t \rightarrow 0} \frac{1 - e^{2t}}{t} = \underline{\hspace{2cm}}$$

$$d) \lim_{x \rightarrow 0^+} x \ln x = \underline{\hspace{2cm}}$$

$$e) \lim_{x \rightarrow \infty} \left( \frac{x+1}{x+2} \right)^x = \underline{\hspace{2cm}}$$