

MATH 152  
Mrs. Bonny Tighe

**EXAM II**  
8.3 – 12.3  
100 points

NAME \_\_\_\_\_

SECTION \_\_\_\_\_ Wed. 10/26/05

1. Evaluate:  $\int e^{-x} \cos x \, dx$

2. Evaluate:  $\int \frac{\sqrt{9 - x^2}}{x} dx$

3. a) Determine the values of  $x$  for which the series is convergent.  $\sum_{n=1}^{\infty} (x - 3)^n$

b) Define each of the following:

- i) a monotonic sequence \_\_\_\_\_
- ii) A convergent sequence \_\_\_\_\_
- iii) a Geometric series \_\_\_\_\_

4. Evaluate:  $\int \sin^3 2x \cos^3 2x \, dx$

5. Evaluate:  $\int \frac{e^{2x} + 1}{e^{2x} - e^x - 6} dx$

6. Determine whether each integral is divergent or convergent and evaluate those that are convergent.

a)  $\int_1^\infty \frac{\ln x}{x} dx$

b)  $\int_{-1}^3 \frac{2}{(x+1)^2} dx$

7. Determine whether the sequence is convergent or divergent. If it converges, find the limit.

a)  $\left\{ \frac{1}{3}, \frac{1}{2}, \frac{3}{5}, \frac{2}{3}, \frac{5}{7}, \dots \right\}$

b)  $a_n = \ln(n-1) - \ln(n+1)$

8. Find the sum for each of the following convergent series.

b)  $\sum_{n=1}^{\infty} \frac{3}{5^n}$

c)  $\sum_{n=1}^{\infty} \frac{1}{n^2 + 3n + 2}$

9. Use the Integral Test to determine whether the series is convergent or divergent.

a)  $\sum_{n=2}^{\infty} \frac{1}{n \ln n}$

b)  $\sum_{n=1}^{\infty} n e^{-n}$

10. Find the length of the arc of the curve  $y = \frac{x^2}{2} - \frac{\ln x}{4}$  on the interval  $2 \leq x \leq 4$

11. Use Simpson's Rule to approximate the area under the curve  $f(x) = xe^x$  from  $x = 0$  to  $x = 4$  with  $n = 8$ .