

1. Find f given the following. a) $f'(x) = \sin x + \cos x - \sec^2 x$, $f(0) = 2$

$$f(x) = -\cos x + \sin x - \tan x + C$$

$$2 = -\cos 0 + \sin 0 - \tan 0 + C$$

$$2 = -1 + C$$

$$3 = C$$

$$f(x) = -\cos x + \sin x - \tan x + 3$$

b) $f''(x) = \frac{6x^3 - 2x}{x}$, $f'(1) = 3$ and $f(0) = 1$

$$f''(x) = 6x^2 - 2, \quad f'(x) = \frac{6}{3}x^3 - 2x + C$$

$$3 = 3(1)^3 - 2(1) + C$$

$$2 = C$$

$$f'(x) = 3x^3 - 2x + 2, \quad f(x) = \frac{3}{4}x^4 - x^2 + 2x + C, \quad C = 1$$

$$f(x) = \frac{3}{4}x^4 - x^2 + 2x + 1$$

c) $f''(x) = 4\sqrt{x} + \frac{1}{x^4}$, ~~$f(1) = 0$~~ and ~~$f(4) = 1$~~ General form

$$f''(x) = 4x^{1/2} + x^{-4}, \quad f'(x) = \frac{4}{3/2}x^{3/2} + \frac{1}{-3}x^{-3} + C, \quad C = -\frac{5}{3}$$

$$f(x) = \frac{8/3}{3/2}x^{5/2} + \frac{-1}{-2}x^{-2} + Cx + D$$

$$f(x) = \frac{16}{15}x^{5/2} + \frac{1}{6x^2} + Cx + D$$

2. A particle is moving with acceleration of $a(t) = \sin t + \cos t$. Find the equation for the position function of the particle if $v(0) = 1$ and $s(0) = 2$.

$$v(t) = -\cos t + \sin t + C$$

$$1 = -1 + 0 + C \quad C = 2$$

$$s(t) = -\sin t - \cos t + 2t + C$$

$$2 = -1 - 1 + C \quad C = 3$$

$$s(t) = -\sin t - \cos t + 2t + 3$$