COURSE: Probability Theory and Stochastic Processes II TuTh 5:30pm-6:45pm in Math & Psychology #105

PROFESSOR: Hye-Won Kang Office: Math/Psychology Building #424 Email: hwkang@umbc.edu Office Hours: Monday during 12:00pm-1:00pm and Tuesday during 10:00am-11:00am, or by appointment. I will try to respond to all emails in the same day. However during the weekends, I am not available to answer them.

**TEXT:** "Introduction to Stochastic Integration", by K.L. Chung and R.J. Williams (Second edition).

# **COURSE DESCRIPTION:**

This course is an introduction to stochastic integration. Audience of the course is expected to have knowledge in introductory probability. We will cover:

- martingales
- stochastic integrations
- Ito formula
- stochastic differential equations

with emphasis on continuous time martingale theory, stochastic integrations, and stochastic differential equations. Intended audiences are graduate students in mathematics and statistics who are interested in probability theory.

### PREREQUISITE:

Basic probability or statistics background is required. Measure theory will be helpful but it is not required. I plan to cover overview of the measure theory during several weeks.

## **GRADING POLICY:**

Grades are based on homework, midterm exam, and take-home final exam. Final letter grade is decided based on the total grade as follows:

Letter Grade	Total Scores	
A	$85 \le \text{Total} \le 100$	
В	$70 \leq \text{Total} < 85$	
С	Total < 70	

However, factors such as overall distributions of grades or consistency in homework will affect on the final letter grade. Contributed portions of the total score are as follows:

	HOMEWORK	MIDTERM EXAM	FINAL EXAM	TOTAL
Percentage	40%	30%	30%	100%

## HOMEWORK:

There will be biweekly assignments and it is due every Tuesday. You are required to turn in your homework to me before the class. All problems in every homework will be graded. You are encouraged to discuss together but copying from other students is NOT allowed. Any violation will result in ZERO grade and will be reported to the University Academic Integrity Committee. Late homework will NOT be accepted.

# MIDTERM AND FINAL EXAMS:

All STAT 622 students are required to take 1 midterm exam and 1 final take-home exam. The midterm exam is during the lecture on Nov 8, 2018. The final take-home exam is due by Dec 17, 2018.

## ATTENDANCE:

The attendance is highly recommended. Based on the previous experience, students who attend every lecture have a very higher tendency to get a higher score at the end. When you come to the class, you are expected to participate in the class. I ask that you are on time and pay attention to the class. No excuse for being habitually late and the use of smartphones during class is strongly discouraged. Please do not distract yourselves and other students.

### **INCOMPLETE:**

If you do complete the course successfully except for a very small portion or a final project due to very extraordinary and emergence situation (such as to stop attending school for the rest of the semester due to injury in an accident), you will be considered to get Incomplete. You are required to submit a written statement and evidence describing reason to get Incomplete. If the reason to get Incomplete is because you are behind in the course, I would recommend to drop the course, instead.

### **ACADEMIC INTEGRITY:**

By enrolling in this course, each student assumes the responsibilities of an active participant in UMBC's scholarly community in which everyone's academic work and behavior are held to the highest standards of honesty. Cheating, fabrication, plagiarism, and helping others to commit these acts are all forms of disciplinary action that may include, but is not limited to, suspension or dismissal. See the Faculty Handbook, or the UMBC Policies section of the UMBC directory. http://gradschool.umbc.edu/students/integrity/

# **APPROXIMATE COURSE SCHEDULE:**

This course will cover various topics. The below is the approximate schedule of the course which is subject to change. The changed schedule will be updated regularly on the course web page in Blackboard.

WEEK	DATES	SECTIONS	TOPICS
1	Tu Aug 28		No class
	Th Aug 30	0-1	Measures and Integrals
2	Tu Sep 4	0-2	Measures and Integrals
	Th Sep 6	0-3	Measures and Integrals
3	Tu Sep 11	1-1	Basic Probability Theory
Wednesd	ay, September	12, is the last da	ay to withdraw from the course <u>without</u>
receiving	a 'W' on your	${f transcript.}$	
	Th Sep 13	1-2	Basic Probability Theory
4	Tu Sep 18	1-3	Basic Probability Theory
	Th Sep 20 $$	1-4	Basic Probability Theory
5	Tu Sep 25	2-1	Definition of the Stochastic Integral
		HW1 due	From Section 0-1
	Th Sep $27$	2-2	Definition of the Stochastic Integral
6	Tu Oct 2	2-3	Definition of the Stochastic Integral
	Th Oct 4	2-4	Definition of the Stochastic Integral
7	Tu Oct 9	2-5	Definition of the Stochastic Integral
		HW2 due	From Section 1
	Th Oct 11	4-1	Quadratic Variation Process
8	Tu Oct 16	4-2	Quadratic Variation Process
	Th Oct 18	4-3	Quadratic Variation Process
9	Tu Oct 23	4-4	Quadratic Variation Process
	Th Oct $25$	5-1	Ito Formula
		HW3 due	From Section 2
10	Tu Oct 30	5-2	Ito Formula
	Th Nov 1	5-3	Ito Formula
11	Tu Nov 6		Review for Midterm Exam
	Th Nov 8	Midterm	Sections $0, 1, 2$ , and $4$
		Exam	
		HW4 due	From Section 4
12	Tu Nov 13		No class
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	Th Nov 15	6-1	Applications of Ito Formula
13	Tu Nov 20	6-2	Applications of Ito Formula
	Th Nov $22$		No class (Thanksgiving day)
14	Tu Nov 27	6-3	Applications of Ito Formula
	Th Nov $29$	1	Stochastic Differential Equations

WEEK	DATES	SECTIONS	TOPICS
15	Tu Dec 4	2	Stochastic Differential Equations
		HW5  due	From Section 5
	Th Dec 6	3	Stochastic Differential Equations
16	Tu Dec 11	4	Stochastic Differential Equations
	Sat Dec 7-17	Final Exam	Sections 4, 5, 6, and Extra materials we covered