

Research Experiences for Math Majors at Arizona State University

Eric Kostelich



ARIZONA STATE UNIVERSITY
SCHOOL OF MATHEMATICAL & STATISTICAL SCIENCES

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Overall philosophy and rationale

- **Mathematical themes:** Uncertainty, prediction, simulation
- **Applications:** Biology, weather/climate, imaging, networks
- **Goals:** Provide a model for 21st Century mathematics curriculum and strengthen connections with other disciplines
- **Professional concern:** We must be able to give compelling reasons to invest in mathematics departments

- Fall enrollment growth: $+21\%$ at 4-year colleges & universities since 1990 (total: **1.6 million** students)
- Math enrollment growth: -2.3%
- All math/stat bachelors degrees: -2%
- Number of bachelor's degrees awarded by doctoral department was up by 41% over 2000 but those by master's & 4-year schools declined by $19-27\%$
- Fraction of 4-year colleges offering Advanced Engineering Mathematics once every 2 years: 7%
Advanced Calculus: 57% Algebra: 52%

The post-Sputnik problem

- Undergraduates see few applications of mathematics after 1950
 - Metropolis algorithm
 - Fast Fourier transform
 - Simplex algorithm
 - Public-key cryptography
 - Kalman-Bucy filter
 - Viterbi algorithm
 - Shotgun genome sequencing
 - etc.
- Resulting #1 FAQ: **What can I do with a math degree?**
- Students should get in-depth exposure to at least one of these topics in their baccalaureate program

My interests and philosophy

- **Professional goals:** Create modern, high-impact programs for mathematics undergraduates that can serve as national models
- Courses and programs to educate mathematically literate scientists (not necessarily more mathematicians *per se*)
- Interdisciplinary collaboration is essential
- Double majors are not worthwhile
- Encourage combined BS/MA programs for strong undergraduates

Undergraduate programs at ASU

- Current enrollment: 72,000 students on four campuses
- About 58,000 undergraduates
- Total mathematics enrollments: 16,000 students in fall, 14,000 in spring
- $\sim 40\%$ precalculus & below; $\sim 30\%$ business math; $\sim 30\%$ in engineering calculus & above
- Approximately 4,000 engineering majors, 550 math majors
- Transfer students, on-and-off enrollment are the rule

The Computational Mathematical Sciences B.S. degree

- **Goal:** Create an interdisciplinary program that would appeal to good science and math students
- Must accommodate transfer students easily
- Encourages summer internships and undergraduate research experience
- Takes a broad view of “scientific computing”

CMS core areas

- **Mathematics:** 3 semester calculus sequence, ordinary differential equations, linear algebra (18 credits total)
- **Science:** 2 one-year sequences in life/physical sciences (16 credits)
- **Computing:** 2 semesters of introductory programming and data structures plus Scientific Computing and Introduction to Numerical Methods (12 credits)
- **Advanced courses:** At least 3 in math/stat and 1 internship/research course (12 credits)
- **Liberal studies:** 5 courses in humanities/social sciences, 2 “science and society” courses (21 credits)

The Scientific Computing course

- **Audience:** advanced undergraduate and beginning graduate students in mathematics and physical sciences
- **Emphasis:** Software development skills for scientific and high-performance computing
- **Topics:** Scripting (shell, Python, makefiles); Fortran 95/2003, C99, C++; OpenMP; LAPACK
- **Prerequisites:** At least 2 semesters of programming, differential equations and/or linear algebra
- The graduate version includes MPI, more on OpenMP, cache coherency, bandwidth issues, etc.

The CSUMS program

- Computational Science Training for Undergraduates in the Mathematical Sciences
- Funded through Divisions of Mathematical Sciences and Undergraduate Education at the National Science Foundation
- Long-term research experiences for cohorts of at least six undergraduates
- From the solicitation: Projects must be genuine research experiences rather than rehearsals of research methods

The CSUMS project at ASU

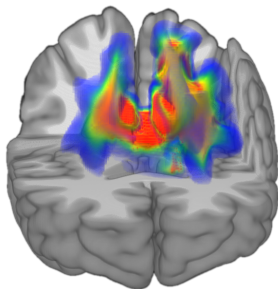
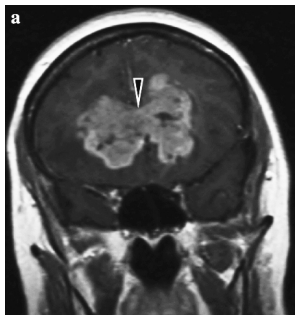
- 65 students in overlapping cohorts since Jan. 2008
- **Basic requirements:** Math major with 3.5+ GPA, differential equations, linear algebra, 1+ semester of programming
- **Year 1:** Weekly pizza seminar
- **Summer 1:** 8-week research projects
- **Year 2:** Weekly pizza seminar, conference, paper, graduation
- **Option:** Continue to BS/MA program
- Conference presentation, possibly an honors thesis or paper

The CSUMS project at ASU, 2

- Sliding window of 12 faculty participants
- 43 CSUMS students have graduated, 18 to PhD programs, 6 masters, 5 BS/MA program, 3 to medical school, 1 to law school
- 20 women, 8 minority, 18 first-generation college students; ages 15–32
- 2 Goldwater Scholars, 1 NSF Graduate Research Fellowship, 3 finalists, 10 local scholarships

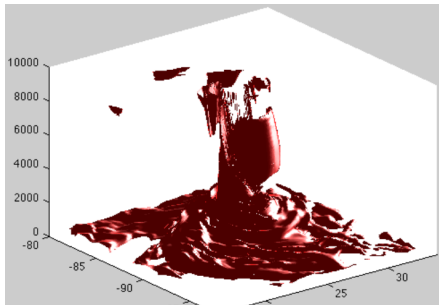
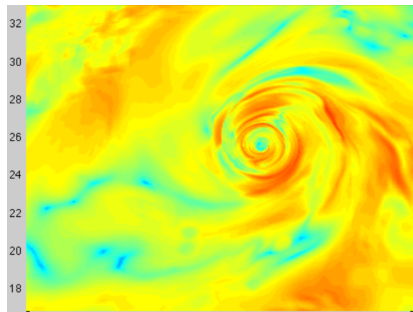
Modeling of glioblastomas (John Ingraham)

- Swanson/Murray model: $g_t = \nabla \cdot (D\nabla g) + \alpha g(1 - g)$
- Use diffusion tensor imaging data to estimate anisotropy



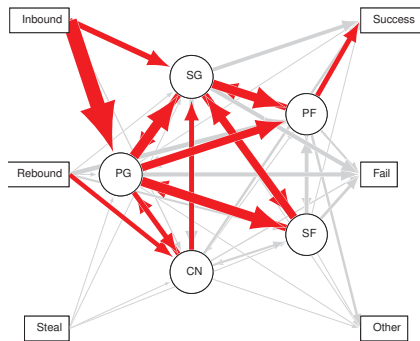
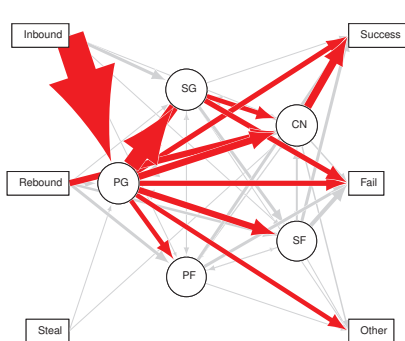
Chaotic saddles in Hurricane Katrina (Chris Wake, Angelica Deibel)

- Weather Research and Forecast model on 128 processors
- Initialized with atmospheric analyses from Aug. 27–29, 2005



Netball: Bulls & Lakers (John Ingraham, Alex Petersen)

- Analyzed every possession of 2010 NBA playoffs
- Passes, inbounds, etc. are links in a graph



- Edge detection from noisy Fourier data
- Financial mathematics (Black-Scholes & variants)
- Rabies epizootics in Arizona and Texas
- Lagrangian dynamics of radioactive particles from Fukushima
- Inverse problems in biofuels
- Astrophysical jets

The MCTP program—beginning July 16

- Partnership with the Maricopa Community College District (141,000 students) and ASU
- MCCCDC enrollments: 5,000 students in precalculus & engineering calculus (up 36% in the last 5 years)
- 3-week, half-day summer enrichment programs at Scottsdale Community College for 20 students
- **Summer 1 program:** Students with Calc I: time value of money, Monte Carlo simulation, logistic growth, Lotka-Volterra models, WFF'n Proof
- **Summer 2 program:** Students with Calc II–III: symmetry & groups, numerical methods, statistical analysis of biological data

- 8-week summer research experience
- Rotating set of “project seminar” courses during the academic year for 18–25 students
- Mathematics and Climate
- Mathematics and Cancer
- Graphs and Networks
- Mathematics and Imaging
- Prerequisites: calculus, linear algebra, differential equations
- Expose students to modern applications of mathematics and provide rationale for the advanced courses

Scaling up

- Jennifer Widom: infolab.stanford.edu/~widom
- 100,000 students signed up for her Introduction to Databases course
- 25,000 submitted assignments, 6,500 finished with a strong score
- Similar effort by Sebastian Thrun for Artificial Intelligence
- Auto-generated multiple-choice tests & Web forums for the masses
- Hand-graded assignments, programming project, written exams, etc. for Stanford students

Why not adopt the Stanford model for CS&E?

- Create a course for 100,000 K–12 teachers on applied math and computational science
- NSF could fund the creation of the initial infrastructure, including semester-long buyouts for faculty at 20–30 colleges & universities to prepare
- The course could be team-taught or be a series of videos by one or two “star” professors
- The format could be adapted for many purposes

The Stanford model, continued

- Each college agrees to offer course credit and charges its regular tuition to cover local expenses for tutoring, homework & exam grading, etc., for those who need continuing ed credits
- “Certificates of completion” could be offered for everyone else who finishes the online portion
- The “textbook” could be a Wiki and sold for 99 cents a chapter (to cover expenses) through iTunes with embedded demos and programmed exercises on an iPad

Acknowledgments

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